

## CLAIMS

We claim:

- 1 1). A method, comprising:
- 2 optimizing an implementation of a programming language, comprising;
- 3 analyzing one or more values computed by a program written in the
- 4 programming language, wherein analyzing one or more values
- 5 comprises;
- 6 representing each bit within a value of the one or more values as an
- 7 abstract element of a lattice having a set of abstract elements
- 8 including  $0_A$ ,  $1_A$ ,  $\perp_A$  and  $T_A$ , wherein the lattice is an abstraction of a
- 9 concrete domain containing 0, 1, and  $\perp$ ;
- 10 analyzing one or more output bits that are produced by an operation in
- 11 terms of one or more input bits that are input to the operation; and
- 12 analyzing the input bits that are input to the operation in terms of the
- 13 output bits that are produced by the operation.
- 1 2). The method of claim 1, wherein optimizing further comprises:
- 2 applying a forward abstract semantic to the abstract element; and
- 3 applying a backward abstract semantic to the abstract element;
- 4 wherein the forward abstract semantic is an approximation of a forward
- 5 concrete semantic including AND, OR, and NOT; and
- 6 wherein the backward abstract semantic is an approximation of a backward
- 7 concrete semantic including  $AND^{-1}$ ,  $OR^{-1}$ , and  $NOT^{-1}$ .
- 1 3). The method of claim 2, further comprising:
- 2 identifying the values within the program as partially constant values.
- 1 4). The method of claim 3, wherein the backward abstract semantic is for a
- 2 complex boolean function including  $LEFT^{-1}$ ,  $URIGHT^{-1}$ ,  $JOIN^{-1}$ ,  $MEET^{-1}$ ,  $LE^{-1}$

and SRIGHT<sup>1</sup>, and wherein the forward abstract semantic is for the complex boolean function including LEFT, URIGHT, JOIN, MEET, LE, and SRIGHT.

5). The method of claim 4, wherein the program is represented in an intermediate language.

6). The method of claim 5, wherein the implementation is a compiler for the programming language.

7). The method of claim 5, wherein the implementation is a computer aided design compiler for the programming language.

8). A computer-readable medium having stored thereon a plurality of instructions, said plurality of instructions when executed by a computer, cause said computer to perform:  
optimizing an implementation of a programming language, comprising;  
analyzing one or more values computed by a program written in the programming language, wherein analyzing one or more values comprises;  
representing each bit within a value of the one or more values as an abstract element of a lattice having a set of abstract elements including  $0_A$ ,  $1_A$ ,  $\perp_A$  and  $T_A$ , wherein the lattice is an abstraction of a concrete domain containing 0, 1, and  $\perp$ ;  
analyzing one or more output bits that are produced by an operation in terms of one or more input bits that are input to the operation; and  
analyzing the input bits that are input to the operation in terms of the output bits that are produced by the operation.

Sub A

FOI: 6552660

1 9). The computer-readable medium of claim 8 having stored thereon additional  
2 instructions, said additional instructions when executed by a computer for  
3 optimizing, cause said computer to further perform:

4 applying a forward abstract semantic to the abstract element; and  
5 applying a backward abstract semantic to the abstract element;  
6 wherein the forward abstract semantic is an approximation of a forward  
7 concrete semantic including AND, OR, and NOT; and  
8 wherein the backward abstract semantic is an approximation of a backward  
9 concrete semantic including AND<sup>1</sup>, OR<sup>1</sup>, and NOT<sup>1</sup>.

1 10). The computer-readable medium of claim 9 having stored thereon  
2 additional instructions, said additional instructions when executed by a computer,  
3 cause said computer to further perform:

4 identifying the values within the program as partially constant values.

1 11). The computer-readable medium of claim 10, wherein the backward  
2 abstract semantic is for a complex boolean function including LEFT<sup>1</sup>,  
3 URIGHT<sup>1</sup>, JOIN<sup>1</sup>, MEET<sup>1</sup>, LE<sup>1</sup> and SRIGHT<sup>1</sup>, and wherein the forward  
4 abstract semantic is for the complex boolean function including LEFT,  
5 URIGHT, JOIN, MEET, LE, and SRIGHT.

1 12). The computer-readable medium of claim 11, wherein the program is  
2 represented in an intermediate language.

1 13). The computer-readable medium of claim 11, wherein the implementation  
2 is a computer aided design compiler for the programming language.

1 14). A system, comprising:  
2 a processor;

Sub A1

FOI: 6552660

3 memory connected to the processor storing instructions for bidirectional  
4 bitwise constant propagation by abstract interpretation executed by the  
5 processor;  
6 storage connected to the processor that stores a software program having a  
7 plurality of separately compilable routines,  
8 wherein the processor optimizes an implementation of a programming  
9 language, by  
10 analyzing one or more values computed by a program written in the  
11 programming language, wherein analyzing one or more values  
12 comprises;  
13 representing each bit within a value of the one or more values as an  
14 abstract element of a lattice having a set of abstract elements  
15 including  $0_A$ ,  $1_A$ ,  $\perp_A$  and  $T_A$ , wherein the lattice is an abstraction of a  
16 concrete domain containing 0, 1, and  $\perp$ ;  
17 analyzing one or more output bits that are produced by an operation in  
18 terms of one or more input bits that are input to the operation; and  
19 analyzing the input bits that are input to the operation in terms of the  
20 output bits that are produced by the operation.

1 15). The system of claim 14, wherein the processor further optimizes by  
2 applying a forward abstract semantic to the abstract element; and  
3 applying a backward abstract semantic to the abstract element;  
4 wherein the forward abstract semantic is an approximation of a forward  
5 concrete semantic including AND, OR, and NOT; and  
6 wherein the backward abstract semantic is an approximation of a backward  
7 concrete semantic including  $AND^{-1}$ ,  $OR^{-1}$ , and  $NOT^{-1}$ .

1 16). The system of claim 15, wherein the processor identifies the values within  
2 the program as partially constant values.

1 17). The system of claim 16, wherein the backward abstract semantic is for a  
2 complex boolean function including LEFT<sup>1</sup>, URIGHT<sup>1</sup>, JOIN<sup>1</sup>, MEET<sup>1</sup>, LE<sup>1</sup>  
3 and SRIGHT<sup>1</sup>, and wherein the forward abstract semantic is for the complex  
4 boolean function including LEFT, URIGHT, JOIN, MEET, LE, and SRIGHT.

1 18). The system of claim 17, wherein the program is represented in an  
2 intermediate language.

1 19). The system of claim 18, wherein the implementation is a compiler for the  
2 programming language.

1 20). The system of claim 19, wherein the implementation is a computer aided  
2 design compiler for the programming language.

1 21). A system, comprising:  
2 means for optimizing an implementation of a programming language,  
3 comprising;  
4 means for analyzing one or more values computed by a program written  
5 in the programming language, wherein analyzing one or more values  
6 comprises;  
7 means for representing each bit within a value of the one or more  
8 values as an abstract element of a lattice having a set of abstract  
9 elements including  $0_A$ ,  $1_A$ ,  $\perp_A$  and  $T_A$ , wherein the lattice is an  
10 abstraction of a concrete domain containing 0, 1, and  $\perp$ ;  
11 means for analyzing one or more output bits that are produced by an  
12 operation in terms of one or more input bits that are input to the  
13 operation; and

14 means for analyzing the input bits that are input to the operation in  
15 terms of the output bits that are produced by the operation.

1 22). The system of claim 21, wherein the means for optimizing further  
2 comprises:

3 means for applying a forward abstract semantic to the abstract element; and  
4 means for applying a backward abstract semantic to the abstract element;  
5 wherein the forward abstract semantic is an approximation of a forward  
6 concrete semantic including AND, OR, and NOT; and  
7 wherein the backward abstract semantic is an approximation of a backward  
8 concrete semantic including AND<sup>-1</sup>, OR<sup>-1</sup>, and NOT<sup>-1</sup>.

1 23). The system of claim 22, further comprising:

2 means for identifying the values within the program as partially constant  
3 values.

1 24). The system of claim 23, wherein the backward abstract semantic is for a  
2 complex boolean function including LEFT<sup>-1</sup>, URIGHT<sup>-1</sup>, JOIN<sup>-1</sup>, MEET<sup>-1</sup>, LE<sup>-1</sup>  
3 and SRIGHT<sup>-1</sup>, and wherein the forward abstract semantic is for the complex  
4 boolean function including LEFT, URIGHT, JOIN, MEET, LE, and SRIGHT.

1 25). The system of claim 24, wherein the program is represented in an  
2 intermediate language.

1 26). The system of claim 25, wherein the implementation is a compiler for the  
2 programming language.

1 27). The system of claim 26, wherein the implementation is a computer aided  
2 design compiler for the programming language.